



# Extend NCEP FV3 to Cover Thermosphere for Whole Atmospheric Modeling

Hann-Ming H. Juang<sup>1</sup>,  
Sajal Kar<sup>1,2</sup>, Adam Kubaryk<sup>1,2</sup>

<sup>1</sup>Environmental Modeling Center, NCEP, NOAA.

<sup>2</sup>I. M. Systems Group Inc.

# Introduction

- The model top of NCEP EMC atmospheric weather and climate GFS is around 60 km.
- To couple with NCEP SWPC space weather models, it requires atmospheric model top to be around 600 km to overlay with SWPC IPE.
- We have extended GSM GFS model top about 10 times higher into whole-atmosphere modeling (WAM), and work for next FV3 GFS

# Opr GFS

vs

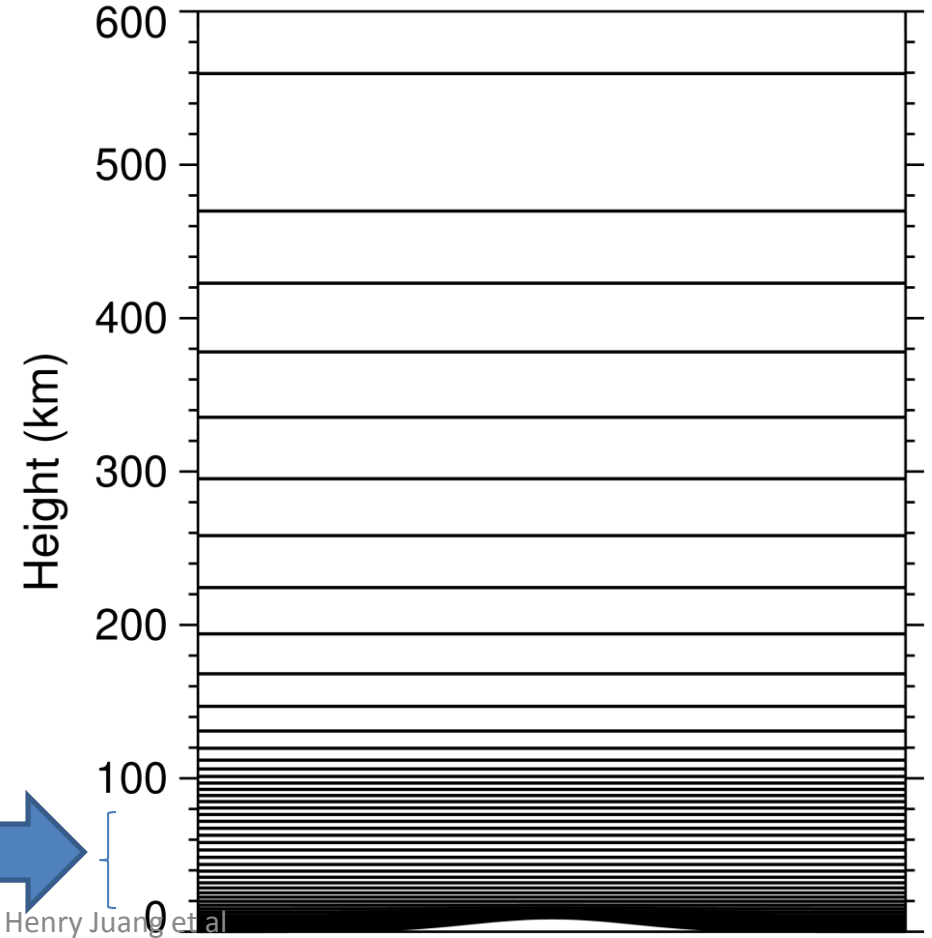
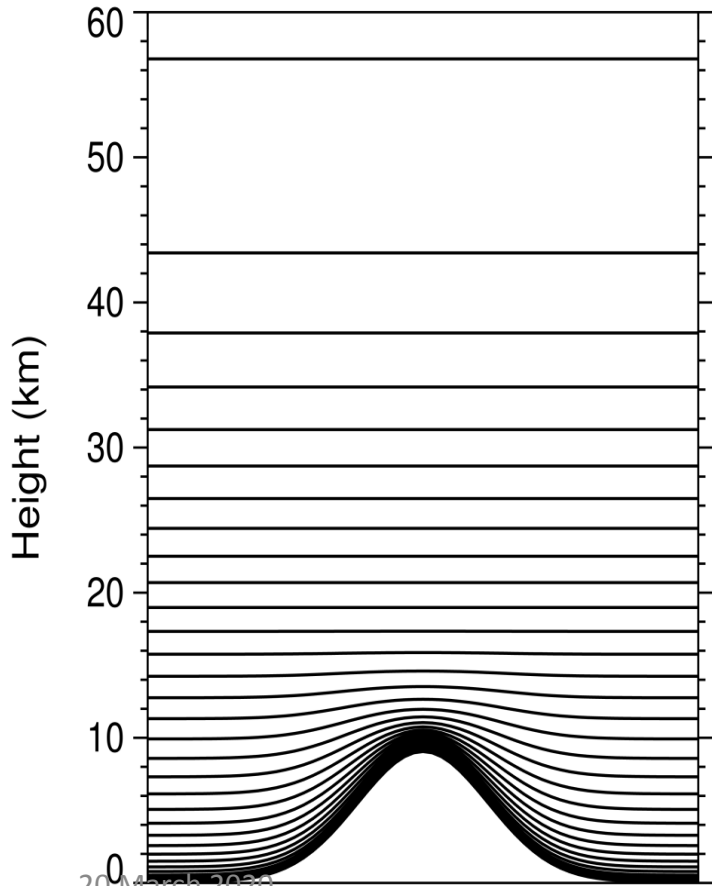
# GSM WAM

64 layers

GFS hybrid vertical grid  
(every 2nd level)

150 layers

WAM hybrid vertical grid  
(every 3rd level)

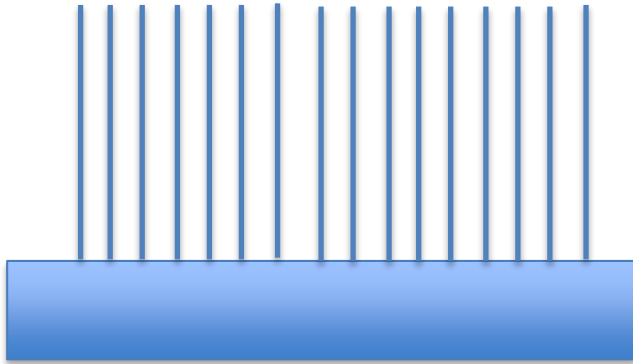


Earth radius  $a=6371\text{km}$ ,  $r=a+z$

## Shallow Atmosphere

Assumption  $r=a$

Op GFS  $z \sim 60\text{km}$   
1% of  $a$



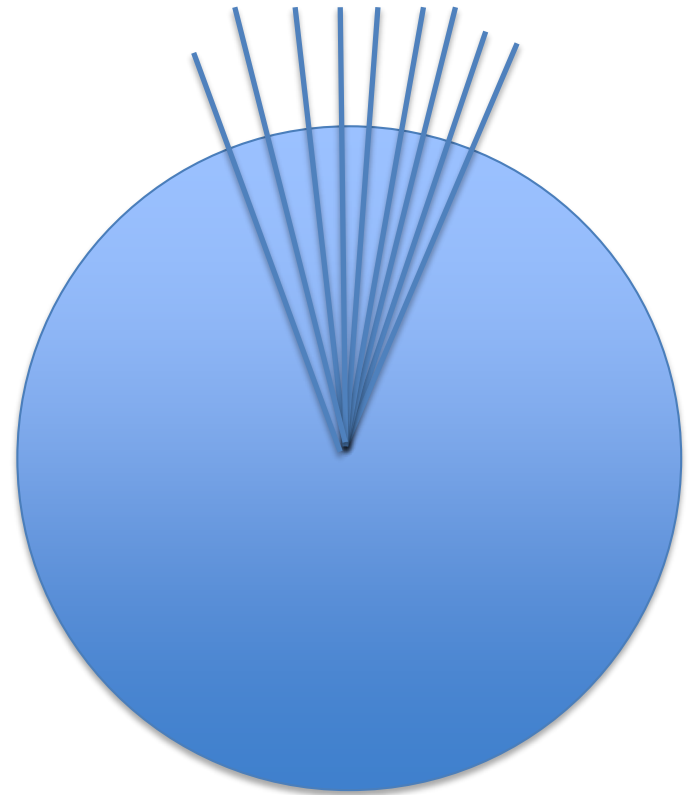
Most of NWP models are shallow-atmosphere dynamics

## Deep Atmosphere

No assumption

$r=a+z$

WAM  $z \sim 600\text{ km}$ , 10% of  $a$



# Deep-Atmosphere Dynamics (DAD)

While it is not  $r=a$

Equations are fully non-approximation and tends to be complicated

$$r = a + z$$

$$u = r \cos \phi \frac{d\lambda}{dt}$$

$$\frac{dA}{dt} = \frac{\partial A}{\partial t} + u \frac{\partial A}{r \cos \phi \partial \lambda} + v \frac{\partial A}{r \partial \phi} + w \frac{\partial A}{\partial r}$$

$$v = r \frac{d\phi}{dt}$$

$$\frac{du}{dt} - \frac{uv \tan \phi}{r} + \frac{uw}{r} - (2\Omega \sin \phi)v + (2\Omega \cos \phi)w + \frac{1}{\rho r \cos \phi} \frac{\partial p}{\partial \lambda} = F_u$$

$$\frac{dv}{dt} + \frac{u^2 \tan \phi}{r} + \frac{vw}{r} + (2\Omega \sin \phi)u + \frac{1}{\rho r} \frac{\partial p}{\partial \phi} = F_v$$

$$\frac{dw}{dt} - \frac{u^2 + v^2}{r} - (2\Omega \cos \phi)u + \frac{1}{\rho} \frac{\partial p}{\partial r} + g = F_w$$

$$\frac{\partial \rho}{\partial t} + \frac{\partial \rho u}{r \cos \phi \partial \lambda} + \frac{\partial \rho v \cos \phi}{r \cos \phi \partial \phi} + \frac{\partial \rho r^2 w}{r^2 \partial r} = F_\rho$$

## DAD in shallowness form without approximation (Juang 2017, NOAA Office Note #488)

A scaled weighted idea was introduced (Juang 2017)

The so-called smily space simplifies the problem, so you can use

$$\tilde{u} = \frac{a}{r} u \quad ; \quad \tilde{v} = \frac{a}{r} v \quad ; \quad \tilde{w} = \frac{r^2}{a^2} w$$

$$\tilde{z} = \frac{r^3 - a^3}{3a^2} = (r - a) \frac{r^2 + ra + a^2}{3a^2}$$

$$\frac{d\tilde{p}}{d\tilde{z}} = -\rho g_0 \quad ; \quad \rho d\tilde{z} = -\frac{d\tilde{p}}{g_0}$$

even

$$\frac{\partial \tilde{p}}{\partial t} + m^2 \left( \frac{\partial \tilde{p}}{\partial \zeta} \tilde{u} + \frac{\partial \tilde{p}}{\partial \zeta} \tilde{v} \right) + \frac{\partial \tilde{p}}{\partial \zeta} \dot{\zeta} = 0$$

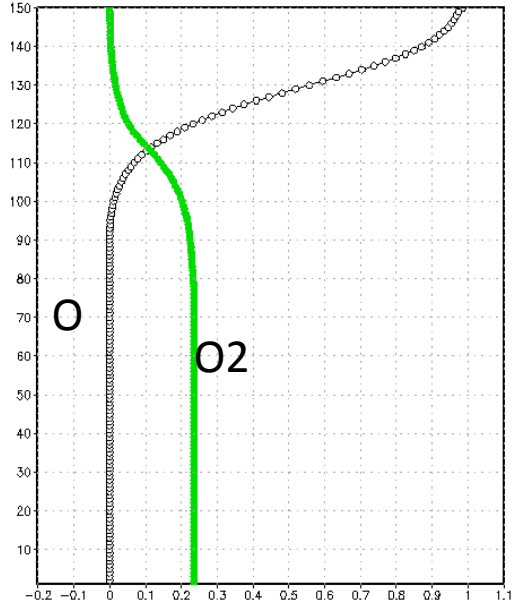
The DAD scaled momentum eqns in shallowness form become

$$\begin{aligned} \frac{d\tilde{u}}{dt} &= -\left(2\frac{\tilde{u}\tilde{w}}{\varepsilon^3 a} + f_c^* \frac{\tilde{w}}{\varepsilon^3}\right)\delta + f_s \tilde{v} - \frac{1}{\varepsilon^2} \left(\frac{1}{\rho} \frac{\partial p}{a \partial \lambda} + \frac{\partial p}{\partial \bar{p}} \frac{\partial \Phi}{a \partial \lambda}\right) \\ \frac{d\tilde{v}}{dt} &= -\left(2\frac{\tilde{v}\tilde{w}}{\varepsilon^3 a}\right)\delta - f_s \tilde{u} - m^2 \frac{\tilde{s}^2}{a} \sin \phi - \frac{1}{\varepsilon^2} \left(\frac{1}{\rho} \frac{\partial p}{a \partial \varphi} + \frac{\partial p}{\partial \bar{p}} \frac{\partial \Phi}{a \partial \varphi}\right) \\ \frac{d\tilde{w}}{dt} &= \left(2\frac{\tilde{w}^2}{\varepsilon^3 a} + m^2 \varepsilon^3 \frac{\tilde{s}^2}{a} + m^2 \varepsilon^3 f_c^* \tilde{u}\right)\delta + g_0 \left(\frac{\partial p}{\partial \bar{p}} \varepsilon^4 - 1\right) \end{aligned}$$

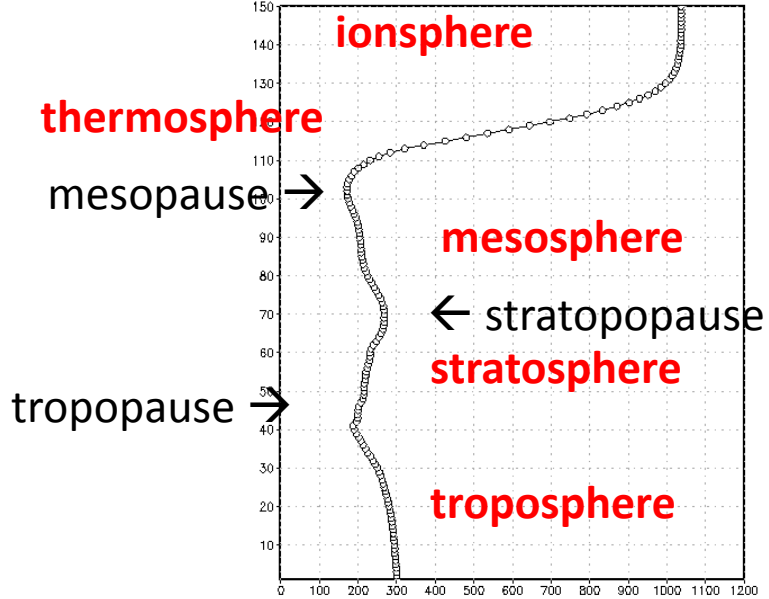
All terms with

$\varepsilon = r/a$  and  $\delta = 1$  are additions to shallow atmosphere dynamics  
 while  $\varepsilon = 1$  and  $\delta = 0$  All eqns are back to shallowness  
 And it is possible to define hydrostatic pressure as  $\frac{\partial \bar{p}}{\partial p} \varepsilon^4 - 1 = 0$

O(white) O2(green) profile for FV3WAM IC

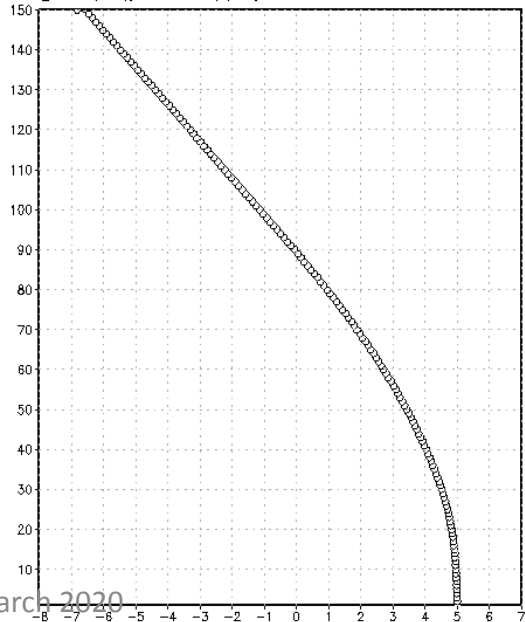


T(K) vertical profile for FV3WAM IC



FV3WAM IC

log10(P(pascal)) profile for FV3WAM IC



FV3WAM Initial Condition

at lat=0 and lon=180

cold start with standard T, P, O, and O2  
other fields, wind, and q are gradually

decreasing to zero at top

top pressure is about 1.E-7 Pa

close to 500~600 km



## Opr GFS

	R	Cp
O3	173.225	820.239
All other dry gases	286.05	1004.60
Water vapor	461.50	1846.00

## WAM

	R	Cp
O	519.674	1299.18
O2	259.837	918.096
O3	173.225	820.239
All other dry gases	296.803	1039.64
Water vapor	461.50	1846.00

$$p = \rho RT = \rho R_d T_v ; \quad T_v = \frac{\sum_{i=0}^N q_i R_i}{R_d} T ; \quad \theta_v = T_v \left( \frac{p}{p_0} \right)^{-\frac{R}{C_p}}$$

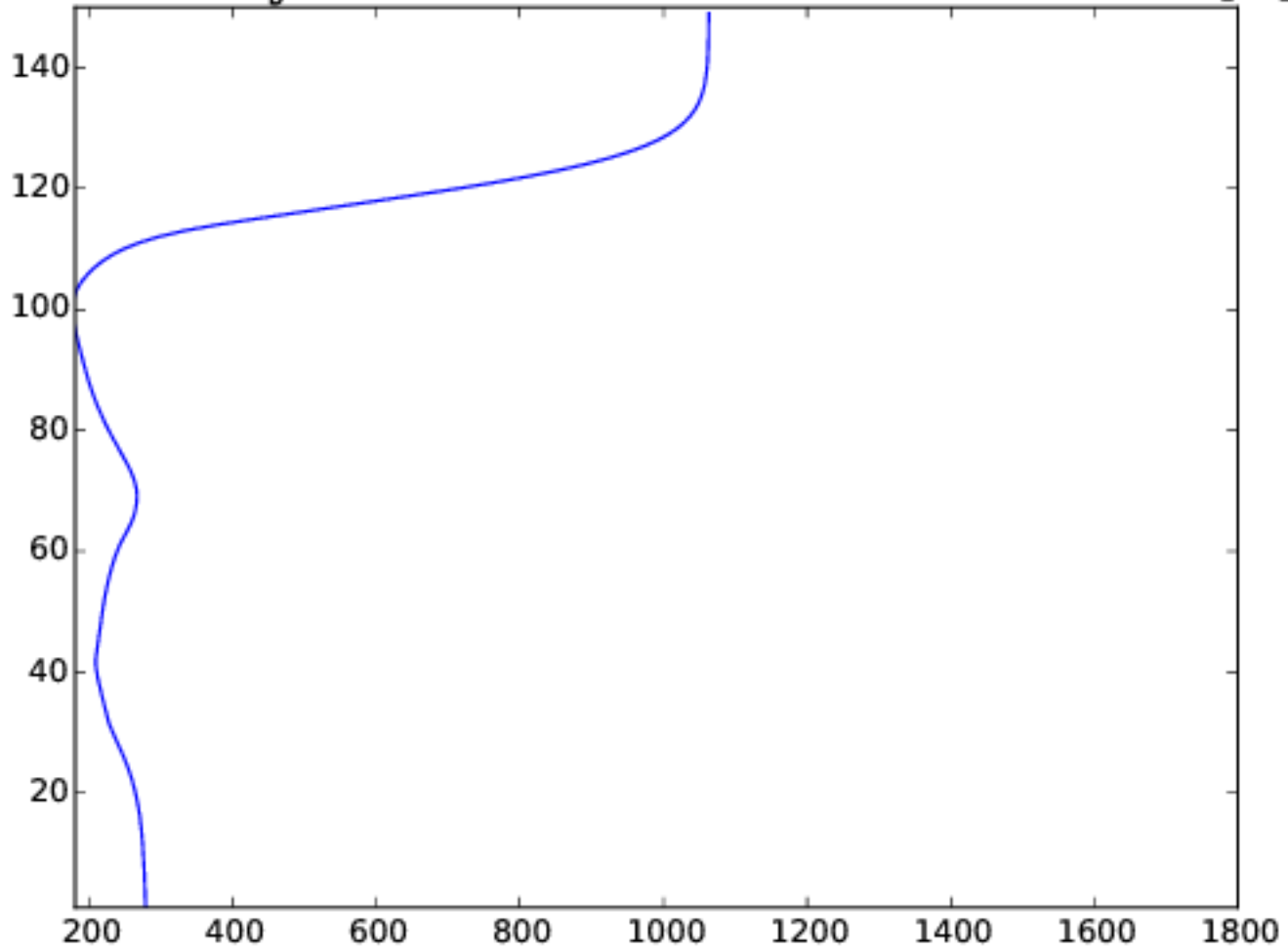
# Implementation steps

- Extend FV3 vertical domain to be the same as GSM WAM
  - Adiabatic mode of FV3
  - Extend to WAM domain with WAM cold-start IC
  - Use GFS physics with Rayleigh damping
  - Implement multi gases thermodynamics
  - Add WAM physics
  - Add diffusivity, conductivity, viscosity for upper-layer integration
  - Add deep-atmosphere dynamics

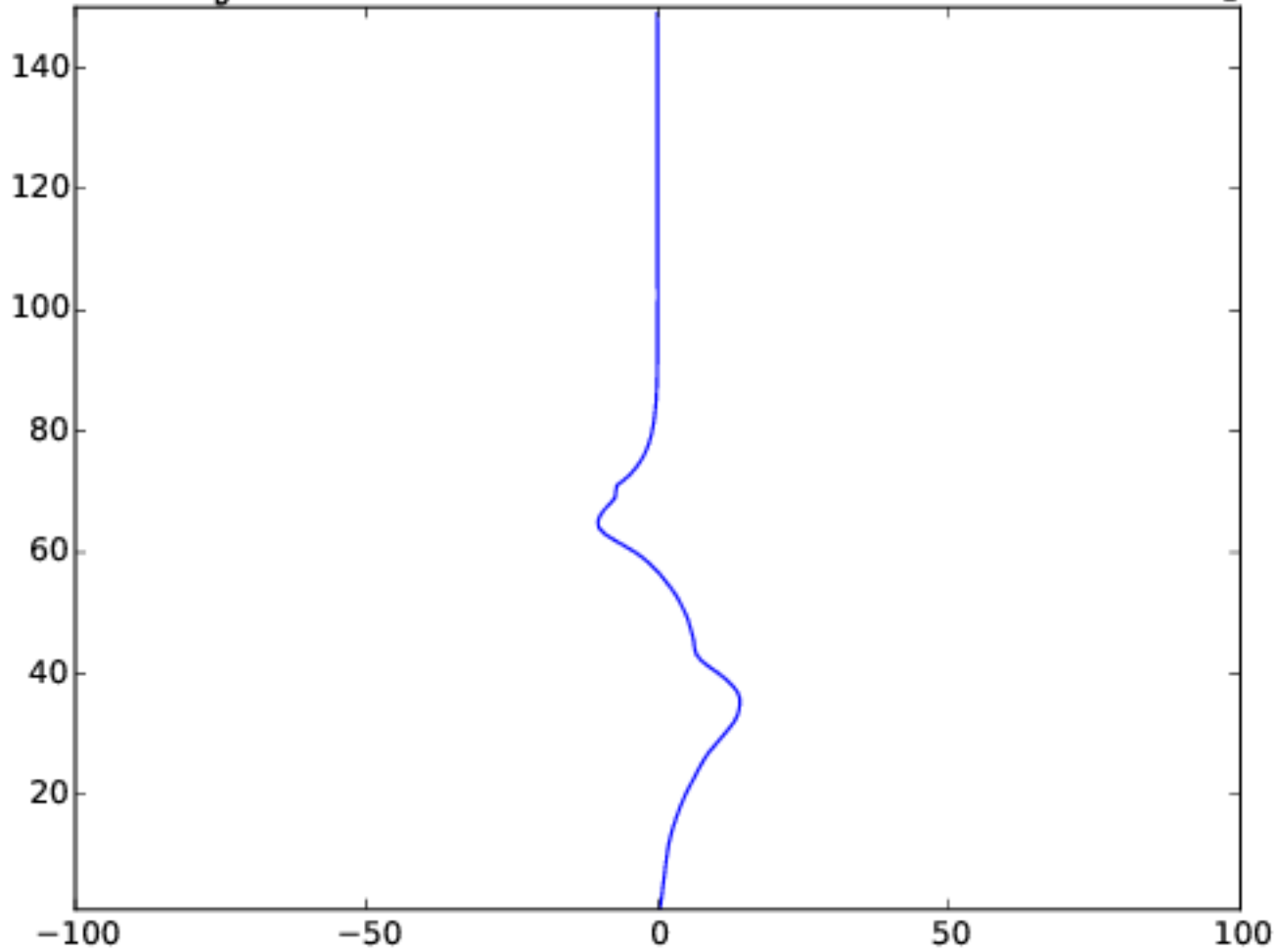
# Adiabatic L149

- Create WAM IC with LEVS=149 through global chgres to run C48 & C96
- FV3 can run adiabatic in weather mode with LEVS=63 about 60km
- However, the same configuration of FV3 cannot run adiabatic mode with LEVS=149 about 600km without stronger Rayleigh damping

Model Layer Mean TEMP at 2017/01/19 06Z [K]



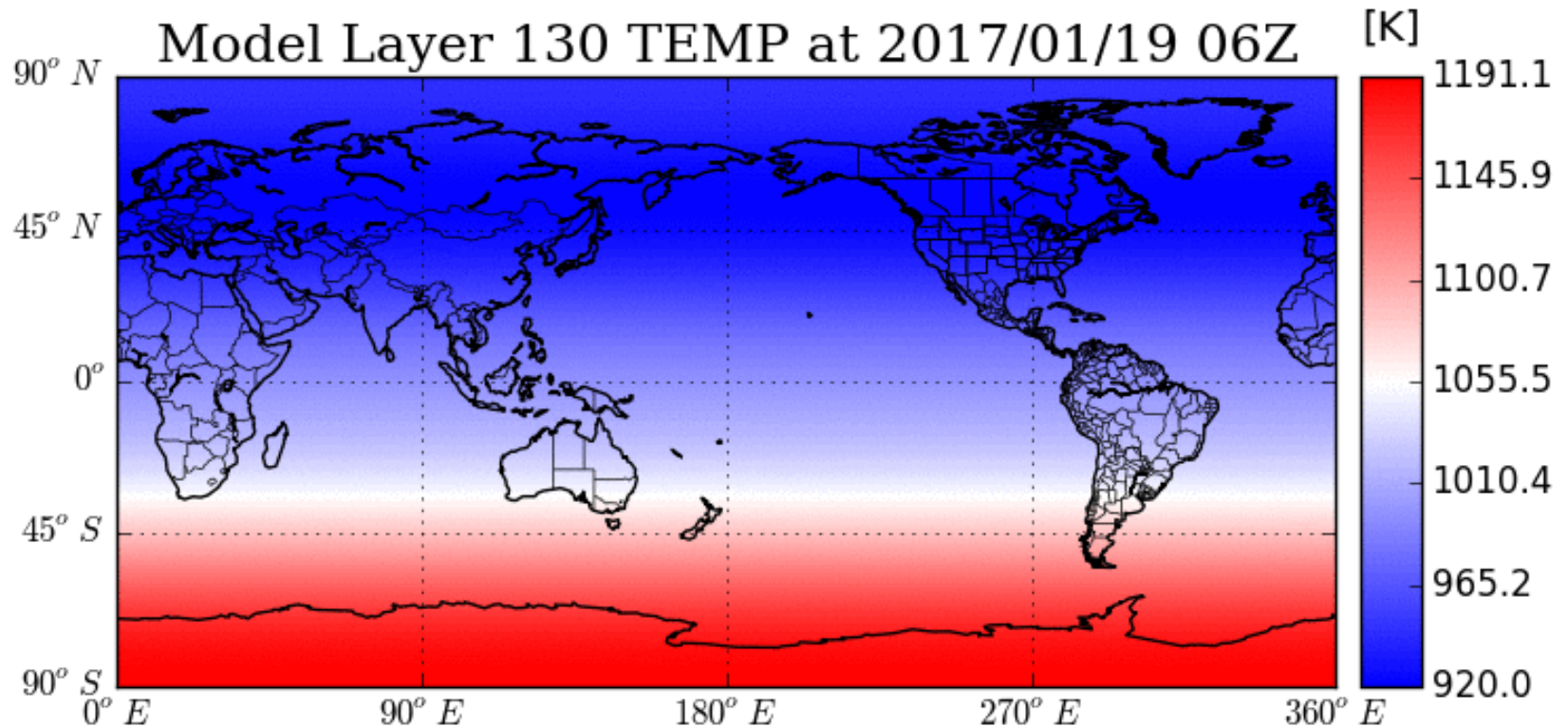
# Model Layer Mean UCOMP at 2017/01/19 06Z [m/s]

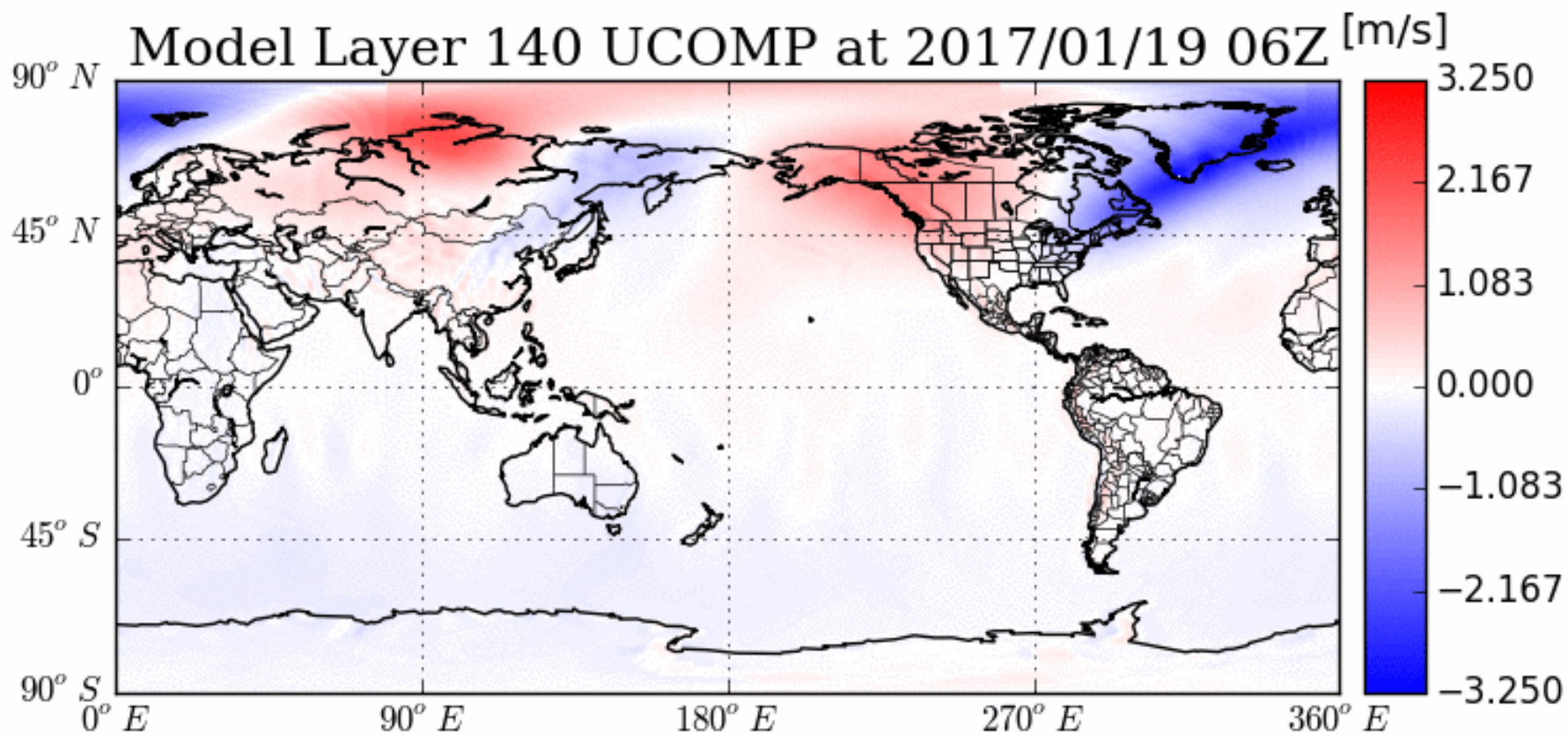


# Turn on GFS physics

- With all namelist option for L149 adiabatic and turn on physics
- Mean upper layers gsm radiation calculation
- Then FV3 can integrate stably with the same Rayleigh damping as GSM
- The WAM physic called IDEA PHYS has not implemented into FV3 yet.

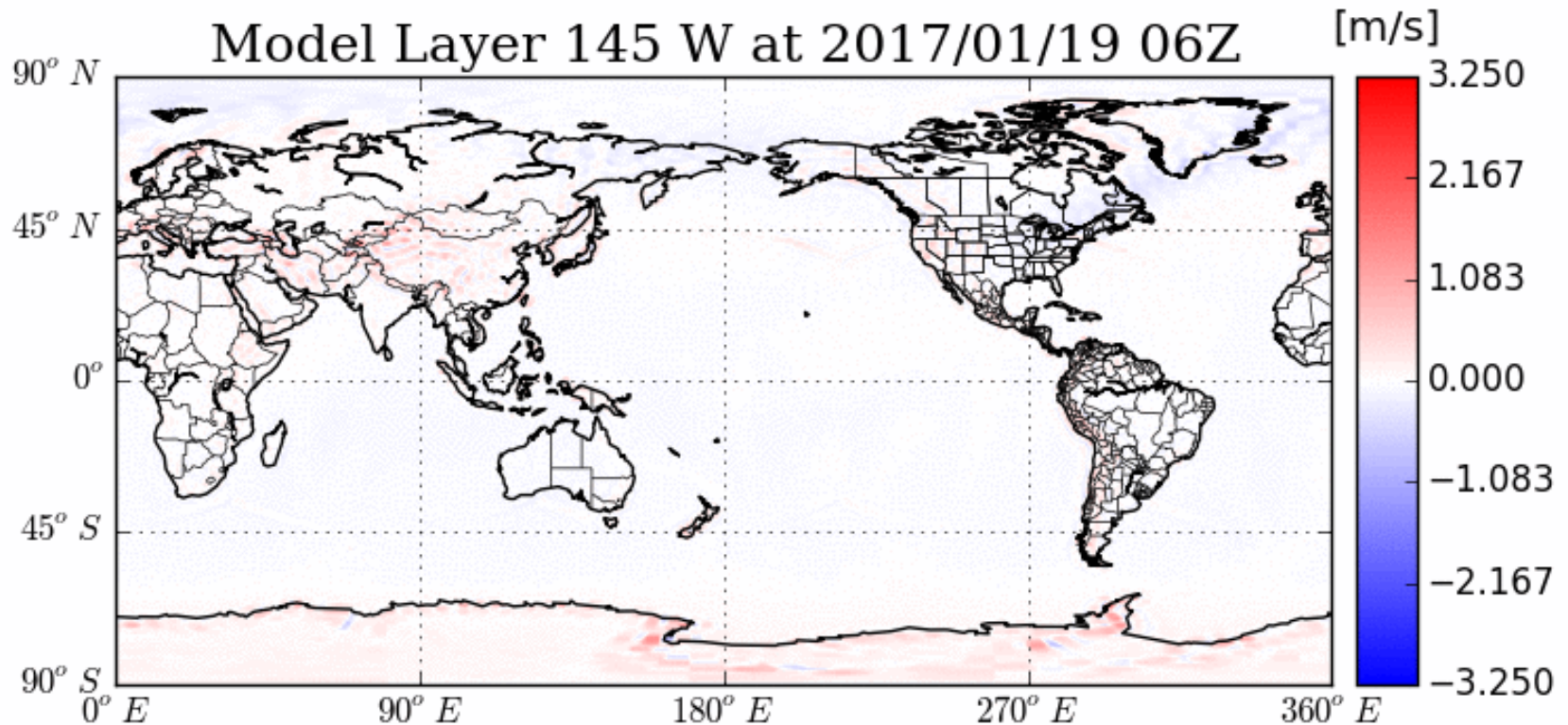
# C96 FV3 L149 gfs-physics with strong Rayleigh damping 5-day integration at layer 130







# C96 FV3 L149 gfs-physics with strong Rayleigh damping 5-day integration at layer 145



# summary

- While extending atmospheric models to whole atmosphere, we consider (1) deep atmospheric dynamics and (2) multi-gases thermodynamics equation.
- FV3 has been extended to WAM with preliminary results of stable integration by Rayleigh damping.
- Multi-gases option has been implemented into FV3 for WAM, and it also benefits to GFS.
- Based on Juang (2017) NOAA Office Note #488, DAD equation can be converted to shallow-atmosphere form without approximation for easy implementation.

# Future Works

- Implement molecular diffusion to remove or reduce the too-much Rayleigh damping for thermosphere wind.
- Implement IPE (Idea) model physics, especially the radiation of multi-gases into WAMFV3.
- Implement deep-atmosphere dynamics, which should be good for WAM as well as GFS.